The Possibility of Earlier LIGO to Detect GW150914

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Abstract

I report the results of my investigation on the sensitivity of LIGO at earlier stages. I took the waveform signal of the event GW150914 to make injections on data from LIGO’s S6 run and recovered them. Overall, none of signal-to-noise ratio values recovered was high enough to claim a detection. In the later portion of S6, where the noise was weaker, the signal could be identified as a candidate event at best. I compared S6 with even earlier stages and found that the earlier ones were also impossible to make this detection.

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I. THE MAIN QUESTIONS

One of the deciding factors that made the detection of elusive gravitational waves possible is the sensitivity of the equipment. Over LIGO’s S5 [1], S6 [2] and O1 [3] (which the scientists previously referred to as S7) runs, the sensitivity was improved significantly each time, with effective attenuation of noise (see section V).

At some degree, the detection seemed very coincidential, for no detection in the past two decades was made until the one made just one week after the testing launch of Advanced LIGO [4]. This leads to some questions: was LIGO at any early stage sensitive enough to make this detection? Was the detection of GW150914 a coincidence?

II. BACKGROUND INFORMATION

More than a century ago Albert Einstein’s General Theory of Relativity stated that we live in a four dimensional world—space-time (three dimensions for space and one for time). Masses cause distortions in space-time, which accounts for the phenomenon of gravity. The theory predicts that changing mass distribution will generally produce ripples in space-time, which is one of his predictions—gravitational waves [5, 6]. For decades, scientists have been struggling to detect gravitational waves from outer space. They upgraded their detectors over and over again, in order to catch the whispers of distant celestial bodies. Fortunately, on September 14, 2015, the LIGO detectors successfully recorded the signals from two colliding black holes, which was the first direct detection of gravitational waves ever, a remarkable one [7]. It is labeled GW150914.

This section aims to provide background information about LIGO and gravitational waves.

A. Introduction to Gravitational Waves

Einstein found that his linearized weak-field equations have wave solutions [7]. These transverse waves are ripples in the fabric of space-time, caused by some strong and catas- trophic events in the universe.

According to Einstein’s calculations, gravitational waves are generated by objects accel- erating with asymmetric motion. To be more precise, gravitational waves require changing

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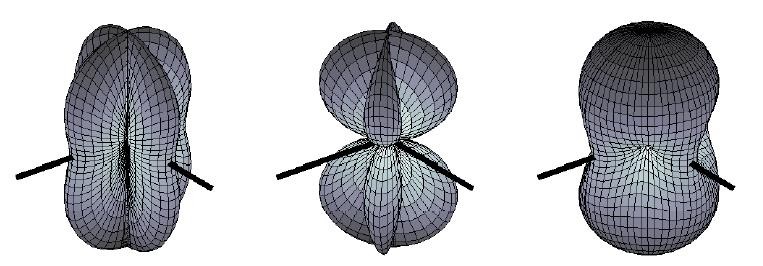


FIG. 1: The pattern on the left is for plus polarization, the middle pattern is for cross polarization, and the right-most one is for unpolarized waves. The black lines are the arms of LIGO detectors, which will be addressed in II B. Source: [9]

quadrupole mass distribution. Generally, the amount of gravitational waves given off is pos- itively correlated with the system’s mass and its speed of motion. Changes in space-time produced by a moving mass are not felt in the distance at once, but they propagate at the speed of light [8].

Gravitational waves are transverse waves, the same as electromagnetic waves, but they are waves of changes in tensors (quadrupole distortions of space-time) which result in ex- pansions and contractions in lengths in certain directions. Unlike the horizontal and vertical polarizations of electromagnetic waves, those of gravitational waves are “plus” and “cross”. However, gravitational waves do share lots of similarities with electromagnetic waves. They have frequencies and wavelengths, whose relationship is given by: λf = c, where λ is the wavelength, f is the frequency, and c is the speed of light. They are able to carry energy, momentum, and angular momentum away from the source [8]. The strain amplitude can be derived from Einstein’s quadrupole formula, and it is inversely proportional to the distance from the mass center [5, 6]. It can also be measured by ratio of the change in length to the original length h = ∆L/L.

Gravitational waves have various sources, but there are mainly four categories: stochastic background, bursts from gravitational collapse, pulsars, and binary systems. Binary systems refer to those that consist of two bodies rotating around each other. Whether or not the two stars collide, gravitational waves will be generated. The detection made on September 14,

2015 is the collision of two black holes, which is called compact binary coalescence—“chirp” September 2016 3

[7]. More details are given by a paper on gravitational waves in section three, in which the author adresses their sources [8].

B. Introduction to LIGO

Distortions in space-time are almost impossible to measure directly, for if you use a meter stick, the meter stick, itself, will expand and contract with changing space-time. Fortunately, light remains the same speed despite any deformation of space-time, which sets the basis for the LIGO detectors [10].

The detector of LIGO—Michelson Interferometer—was invented by Albert Abraham Michelson. The Micelson Interferometers were first applied in the famous Michelson-Morley experiment [11]. Its function is for optical interferometry. With a beam splitter, a light source is split into two arms, and each of the new beams is reflected back and combined again. The result of such combination leads to optical interference—either constructive or destructive–depending on the changes in the length of the arms. Therefore, the photo detector could sense the variation in the arm lengths [10].

The interferometer in LIGO consists of two vacuum arms of equal length—4 kilometers long, forming an L shape. There is a laser light source and a photodetector at the corner of the L, as well as a beam splitter. At each end and in the middle of the arms are four freely-hanging mirrors which reflect the laser beam, and the two beams are combined into one at the beam splitter. Those mirrors in the middle are used to increase the distance that light beams travel, and as a result, the actual effective length is increased from 4km to 1120 km, greatly enhancing LIGO’s sensitivity. If the arm length were to change, the two light beams that were originally in phase would be out of phase, creating destructive interference, which allows the photodetector to sense the infinitesimal change in the length of the arms [10, 12].

Moreover, the two LIGOs in the US are located in Livingston Parish , Louisiana and Hanford, Washington. Both are L-shaped and of the same size–their arms are all 4km long. The two Ls are in different directions, and they are separated by 3030.3 kilometers on land, which means the planes that these observatories are on form a nonzero dihedral angle [33]. Therefore, it is guaranteed that gravitational waves from any directions can be detected, given enough sensitivity.

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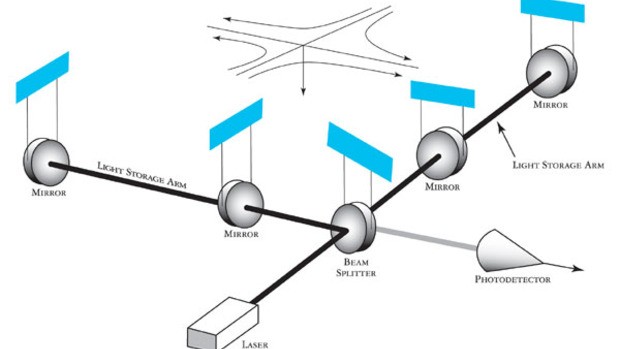


FIG. 2: Basic schematic of LIGO’s interferometers with an incoming gravitational wave depicted as arriving from directly above the detector. Source: [10]

A brief history of LIGO is given on a website by Caltech [13]. A more technically and quantitatively detailed description of LIGO is given by the paper on LIGO’s instruments [9].

C. Sensitivity of the Detectors

Similar to any real physics experiment, the LIGO detectors face various disturbances from the environment. Considering the small amplitudes of gravitational waves, we see that sensitivity become decisive. At the very beginning of the construction, the interference of the noises is so high that it was impossible for the detectors to collect data clean enough to analyze. But the quality of data collected has been significantly improved over the several stages of LIGO. The datasets of its S5 (2005-2007) [1], S6 (2009-2010) [2], and O1 (2015 September-2016 January) [3] are available online [14]. Among all these sensitivity- limiting factors are primarily: seismic noise (at relatively low frequencies), thermal noise (at mid frequencies), shot noise (at high frequencies), and the problems with the lasers and electronics. Some more specific details, including solutions, are given by [15–17]

The problems related to sensitivity are curious to investigate. My research is closely related to sensitivity.

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D. Injections

In short, injections are used to test whether the detectors were working well. There are two types of injections: hardware injections and software injections. The first type is made by manually changing the position of the mirrors in the interferometer. The second type is achieved by adding a signal directly into the data flow. Moreover, there were those called “blind injections”, when few scientists knew it was an injection while the majority were convinced that it was a real detection. One of the most famous events was in 2010, which was reported on the LSC news site [18].

III. PREPARATION OF DATA FILES

The strain data of the GW150914 event is obtained from the LOSC site. Specifically, it is stored as a waveform.txt file from the “Download the Data” section of the LOSC tutorial [19]. This strain data was later used as the signal for the software injection.

As for the template for injection recovery, it is different from the waveform. It is included in the zip file of another tutorial [20]. The complex template contains two waveforms, one of which is used as the real part and the other as the imaginary part. Moreover, as pointed out in the “Waveform Template” of this tutorial, the templates are not 100% identical to what the scientists actually used. Many subtleties are skipped, for example. But the quality of the templates online is good enough for my investigation. Note that this was different from the strain data for making the injection.

The background strain data of the injections were selected from a number of datafiles in the “H1” detector from LIGO’s S6 run, from GPS time 931035615 to 971622015. The S6 data archive is available on the LOSC site as well [21]. Because of the probable fluctuation in the power of the background noise over the entire S6 run, 10 different and relatively evenly dispersed data files were chosen, each starting at GPS time 931127296 (0.226%), 934846464 (9.39%), 941707264 (26.3%), 941785088 (26.5%), 947154944 (39.7%), 952623104 (53.2%),

959344640 (69.8%), 963629056 (80.3%), 967442432 (89.7%), and 971407360 (99.5%), all lasting for 4096 seconds. The files will be referred to with numbers from 1 to 10, respectively.

The quality of background noise is critical. A piece of low-quality data could result in a misleading outcome. Furthermore, those kind of datafiles would be vetoed by the scientists.

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As a result, even if there really were an event, the segment it lies in would not be searched. And it would be useless to do investigate on such a datafile. In general, the background being injected on should have the proper data quality flags on. Because the event of GW150914 is a compact binary coalescence system [7] and the mass is big enough to be categorized as “high mass” [22], the flag of “CBCHIGH CAT4” should be on. Besides, there should not be any other injections which would affect my recovery, so the flag of “HW” should be off [23]. The specific way to slice qualified data segments is given in the code in appendix section IX.

The process of gathering the raw data for analysis could be categorized into two steps—making and recovering the software injection. The injections were made by simply superposing the waveform onto the background signal. Five injections were made into each of the ten datafiles at randomly selected points. In addition to the original strain, the waveform signal was amplified by factors ranging from 2 to 30, with a serial interval of 2, and was injected at the same points as those for the unamplified signal. In total, that was 800 injections. To recover the injection, signal-to-noise ratio (SNR) [24] of each injection was computed with matched filter [25]. In addition, another set of recoveries were done with no injections in the datafile, which served as a check of the false alarms, the details of which will be addressed in section IV B. That was 850 SNR values in total. The signal processing was almost entirely the same as that in the tutorial on LOSC site [19]. The exact python code is given in the appendix section IX with more detailed description.

IV. DATA ANALYSIS

This section presents the data analyzing process.

A. Computing the RMS of Strain Data

In this case, the root mean squared (RMS) [26] of strain data functioned as a representa- tion of the significance of the noise in each datafile. It can be inferred from the RMSs that noise in the detectors is generally louder in earlier stages of S6 than in later ones.

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TABLE I: RMS calculated from each raw datafile.

File Number 1 2 3 4 5 6 7 8 9 10

RMS (×10−17 ) 15.0 7.68 10.3 8.84 8.72 9.27 5.33 2.64 4.91 3.30

B. The Mean SNRs

As stated in section III, there are in total 850 SNRs computed from matched filter corresponding to 17 different amplifications, including an amplification of zero (recovering from uninjected strain data). The SNRs computed from the same amplification of the signal in one datafile were calculated the average value. These mean values were further sorted into 10 series, each for a single file.

In fact, the SNRs recovered were all time-varying functions. What actually matters is the local maximum of each function. As a result, the SNR value recovered from the raw strain data was a high partial or accidental matching of the background noise to the template. However, it served as a decent indication of the minimum SNR value that could have been a false alarm in each datafile. In other words, if the maximum SNR value is not sufficiently higher than that calculated from raw strain data, that SNR is probably a false alarm. As it turns out, what was recovered from raw data was quite close to that recovered with an original signal, which can be seen from the first two points of each series in the scatterplot in Figure 3.

Consequently, the SNRs recovered from the unamplified injection (or amplification equals one) are largely unreliable, so there should be another method of calculating the SNRs should be, which was to use regression analysis to extrapolate the SNRs of the injected signal at original amplitude.

C. Computing the Linear Regression

Due to the nature of SNR, the amplification (signal power) should be positively correlated with the output. From Figure 3 it can be seen that the y and x values are not only positively correlated, but they have a nice linear relationship. Therefore, linear regression [27] was chosen as the model.

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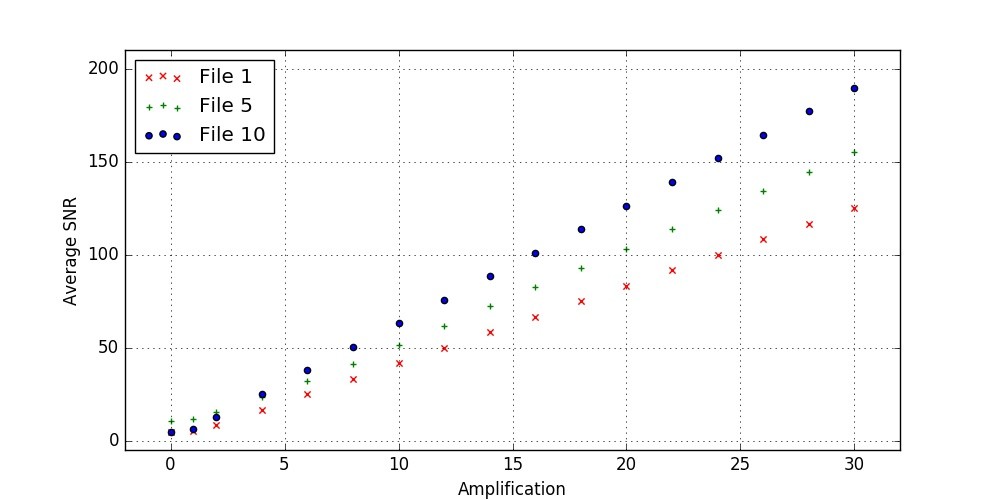


FIG. 3: A selected representative scatterplot—mean SNR plotted against the amplification of injected signal—generated by matplotlib.pyplot. The plots are the average maximum SNR values computed from each file at various amplifications of signals. There are three out of the ten series plotted. They represent the early, middle, and late stage of S6. One can see from Table I that file 1 contains the most noise, the noise in file 5 is among the middle, and file 10’s noise is the second least.

Before the computation of each linear regression, all of the data points at the first four amplifications were excluded, because they are not clean enough. In Figure 3, it can be seen that the first four points of each series cross and overlap each other. The reason for this such unclearness is probably the relatively high ratio of the strength of the background noise to that of the signal.

In general, the statistics in Table II make good sense. The fourth column of figures (R2)

indicate the fitness of my model: the closer the value is to one, the better the statistics fit the model [28]. That these values are so close to one the model had been well chosen, and thus the extrapolations would be quite accurate. In addition, the intercept are also very close to zero. Because SNR is the relative power of the signal over the background noise, it should theoretically be zero if there is no signal present. In reality, however, the SNR is never zero because of noise’s partial matching with the template. Now that the intercept are close to zero, the extrapolations have become more credible.

Finally, since the model of linear regression in this case is simply SN R = Amplitude ×

Slope +I ntercept, the mean SNR at amplification equals one were easily extrapolated, which

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TABLE II: These are the statistics calculated from the mean-SNR series in section IV B by

linear regression. The fifth column lists the extrapolations.

File Number Slope Intercept R2 Extrapolated Mean SNR

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| 1 | 4.167 | -0.073 | 0.999999999511 | 4.094 |
| 2 | 4.371 | 0.093 | 0.999999985140 | 4.464 |
| 3 | 4.171 | -0.692 | 0.999999992354 | 3.479 |
| 4 | 5.151 | -0.487 | 0.999999995775 | 4.664 |
| 5 | 5.155 | 0.134 | 0.999959583093 | 5.290 |
| 6 | 6.164 | -0.042 | 0.999999998879 | 6.122 |
| 7 | 6.279 | 0.206 | 0.999999998734 | 6.485 |
| 8 | 5.953 | 0.178 | 0.999999998084 | 6.131 |
| 9 | 6.032 | -0.036 | 0.999999997650 | 5.996 |
| 10 | 6.328 | -0.201 | 0.999999999774 | 6.128 |

gave the values in the fifth column in Table II. Therefore, the predicted maximum SNRs of GW150914 signal in the background noise of LIGO at various stages over S6 run were found. Overall, none of those SNRs would be significant enough to claim a detection. In the early stages where noises were high, the signal would be overwhelmed by the noise, while in the late stage where noises had been reduced, the maximum SNR is still not significant enough. One can see from Figure 4 that the SNR function of background noise is constantly around four with some spikes up to 6, regardless of that maximum around 3500 seconds due to hardware injection. Moreover, the SNR time functions in other nine files look very similar, all with SNR values of four for most parts and a few spikes up to about six.

V. COMPARING S6 TO EARLIER STAGES OF LIGO

As the sqare root of power spectral density [29], amplitude spectral density (ASD) can serves as an indication of the amount of background noise as well. Figure 5b suggests that the sensitivity of LIGO during S5 is not any better than that during S6, and Figure 5a strongly suggests that the overall sensitivity of LIGO had been improved over time. As a result, it would be impossible for LIGO at stages prior to S6 to detect GW150914, for even

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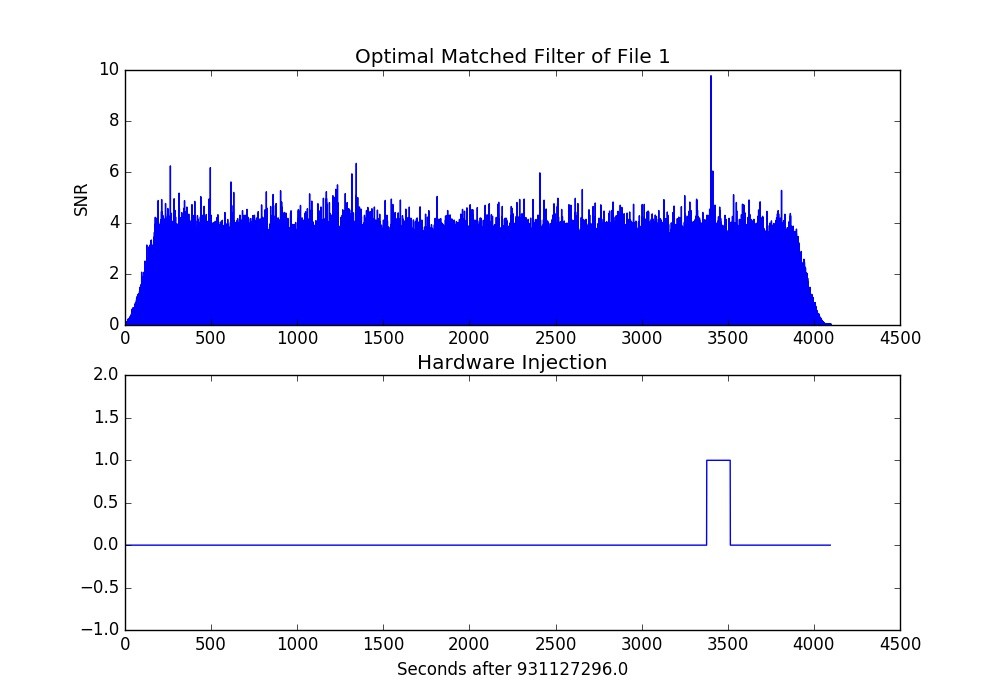


FIG. 4: The upper image is the SNR function over the full span of file one. The lower image flags a hardware injection where there is a bulge in the graph. The highest spike in the upper graph is due to an injection indicated by the lower graph.

the sensitivity at S6 was not high enough.

VI. SIDE EVIDENCE

In fact, the subsequent successful detections of both a gravitational-wave event (GW151226) [31] and a gravitational-wave candidate event (LVT151012) [3, 32] also serve as evidence that the detection of GW150914 was not a coincidence. One can infer from these detections that the newest LIGO had finally been sensitive enough to make frequent detections. It appears that more detections will come in the near future.

VII. CONCLUSION

I found that the GW150914 event would not be loud enough for LIGO at S6 run to detect. The signal could, at best, be identified as a candidate event at later stages where the sensitivity was relatively better, but its significance would be far from enough to claim a real detection. In short, LIGO in the S6 run was not sensitive enough to make this detection,

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(a) Sensitivity of LIGO from S1 to S5 (b) Sensitivity of LIGO at S5 and S6

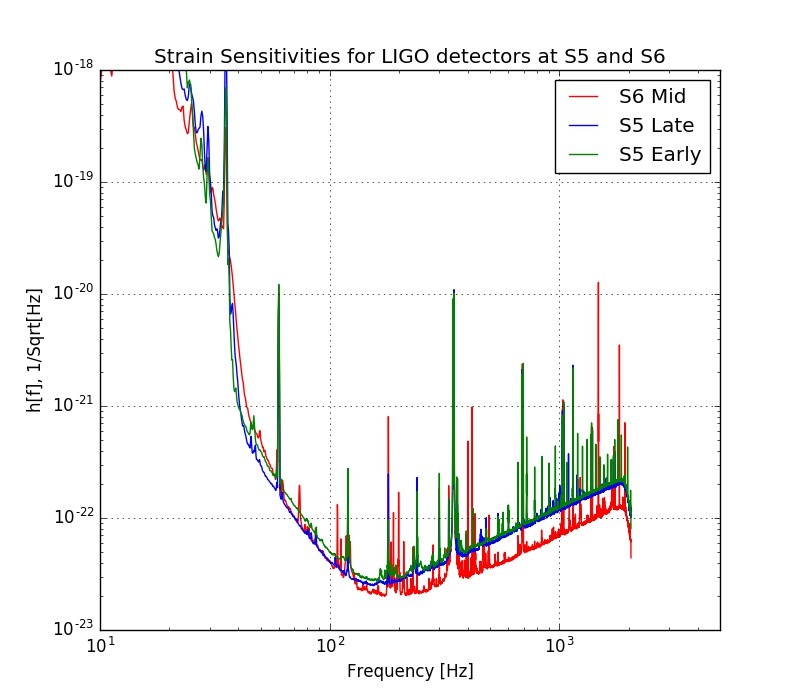
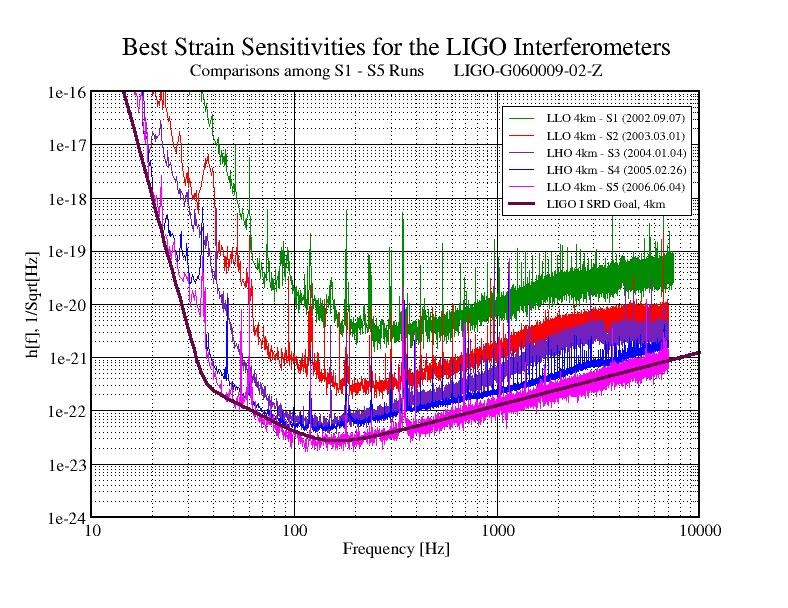


FIG. 5: Left: a set of amplitude spectral density graphs of the backgound noise of LIGO during the five runs prior to S6. Source: [30]. Right: the amplitude spectral density graphs of three strain data pieces during S5 and S6, computed by matplotlib.mlab.psd() and generated by matplotlib.pyplot The three files (S6 med, S5 late, and S5 early) are from the H1 detector and start at GPS time 947154944, 875126784, and 822124544.

not to mention the stages (like S5) prior to S6, where sensitivity was even worse. Besides, the other two subsequent detections have made it more likely that detecting GW150914 was just a beginning of a series of detections, triggered by the increased sensitivity. In conclusion, the detection of the GW150914 event was not a mere coincidence. In contrast, the successful detection was (and future detections will be) made possible by persisting in upgrading the detectors.

VIII. EXTENSION

Although the results indicate that earlier LIGO was not able to detect GW150914, it may become possible if the parameters that decide the strain amplitude of the gravitational waves were to change. As stated in section II A, the strain amplitude of gravitational waves measured at a certain point is inversely proportional to the distance from the source. Thus, if the distance from the binary system of GW150914 were to be halved, the amplitude of the signal would be doubled (or amplified by a factor of two). According to the regression

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model in section IV C, the expected maximum SNR would be around ten, indicating a highly probable event. However, that would also mean the total number celestial bodies within the radius would be cut to roughly one eighth of the original number. Given the nonuniform distribution of stars and galaxies, the probability that a similar system exists within a shorter radius is hard to predict. More investigation and presumably future detections will

be needed to resolve this problem.

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[33] Given by the scaler in Google Earth

IX. APPENDIX—PYTHON SCRIPT

This is the main Python script used for my research. Please note that an automatic line break in this paper would cause an absence of line break operator “\” or a line without the comment notation “#” when one copies the script to a compiler.

First, the program completed the recovery on uninjected data. Then it superposed the unamplified data at five random points and did the same recovery. Then, instead of starting from raw data, it just superposed another signal with an amplification equal to the differ- ence from the current one to the next one, and the program did the recovery for the next amplification. For example, if the program was now at an amplification of 10 and the next one was 12, it just superposed five signals amplified by a factor of two to the five according points.

This version is 2.7. In addition, the code was compiled and run by Anaconda2 (iPython). The total computational time was about 38 minutes.

# Programmer: Tony Lu Zhehao

# From: 2AP2 International Cirriculum Center,

# Shenzhen Foreign Languages School, Shenzhen, China

# This script is to make and recover injections on LIGO’s raw datafiles.

# It generally randomly pick 5 points in each datafile to work on.

# The recovery algorithm is adapted from the tutorial of GW150914 on LOSC.

# It has been very slightly altered, but 99% of it is the same.

# URL: https://losc.ligo.org/s/events/GW150914/LOSC\_Event\_tutorial\_GW150914.html

# NOTICE:

# Highly recommend backing up the files, because the injections will not be

# easily removed.

# The output is the average SNR of each injection.

**import** h5py

**import** numpy as np

**import** matplotlib.pyplot as plt

**import** matplotlib.mlab as mlab

**import** scipy.signal as sig

**import** readligo as rl

**from** random **import** randint

#-- Sampling rate equals to 4096 Hz

fs = 4096

#-- Read in the waveform

temp\_time, temp\_strain = np.genfromtxt(’GW150914\_4\_NR\_waveform.txt’).transpose()

#-- Read in the template

f\_template = h5py.File(’GW150914\_4\_template.hdf5’, ’r’)

template\_p, template\_c = f\_template[’template’].value

template = template\_p + template\_c \* 1.j

# to remove effects at the beginning and end of the data stretch, window the data

# https://en.wikipedia.org/wiki/Window\_function#Tukey\_window

**try**: dwindow2 = sig.tukey(template.size, alpha=1./8) # Tukey window preferred, but requires

recent scipy version

**except**: dwindow2 = sig.blackman(template.size) # Blackman window OK if Tukey is not

available

# the length and sampling rate of the template MUST match that of the data.

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datafreq = np.fft.fftfreq(template.size)\*fs df = np.**abs**(datafreq[1] - datafreq[0])

# prepare the template fft.

template\_fft = np.fft.fft(template\*dwindow2) / fs

# -- To calculate the PSD of the data, choose an overlap and a window (common to all detectors)

# that minimizes \enquote{spectral leakage} https://en.wikipedia.org/wiki/Spectral\_leakage

NFFT = 4\*fs

psd\_window = np.blackman(NFFT)

# and a 50% overlap:

NOVL = NFFT/2

#-- Set the amplifications of signal to be injected

A = [0,1,2] + **range**(4,31,2)

#-- Define the function to segment the segments into suitable segments

**def** slice\_filter(dq, hw):

#-- Cut the whole segment in to small ones of 60s, with spacing of 1s

i = 0

**while** i < **len**(dq):

**if** dq[i].stop - dq[i].start < 32\*fs:

**del** dq[i]

**continue**

dq.insert(i, **slice**(dq[i].start, dq[i].start + 32\*fs))

dq[i+1] = **slice**(dq[i].stop + 1\*fs, dq[i+1].stop)

i += 1

#-- Delete the segments with injection activated

i = 0

j = 0

**if len**(hw) == 0:

**return** dq

**while** i < **len**(dq) **and** j < **len**(hw):

#-- dq is 100% before hw

**if** dq[i].stop < hw[j].start:

i += 1

#-- dq is 100% after hw

**elif** dq[i].start > hw[j].stop:

j += 1

#-- dq and hw overlap

**else**:

**del** dq[i]

**return** dq

#-- Prepare the files to work on

fileName = []

fileName.append(’H-H1\_LOSC\_4\_V1-931127296-4096’)

fileName.append(’H-H1\_LOSC\_4\_V1-934846464-4096’)

fileName.append(’H-H1\_LOSC\_4\_V1-941707264-4096’)

fileName.append(’H-H1\_LOSC\_4\_V1-941785088-4096’)

fileName.append(’H-H1\_LOSC\_4\_V1-947154944-4096’)

fileName.append(’H-H1\_LOSC\_4\_V1-952623104-4096’)

fileName.append(’H-H1\_LOSC\_4\_V1-959344640-4096’)

fileName.append(’H-H1\_LOSC\_4\_V1-963629056-4096’)

fileName.append(’H-H1\_LOSC\_4\_V1-967442432-4096’)

fileName.append(’H-H1\_LOSC\_4\_V1-971407360-4096’)

#===========================#

#========Main Part==========#

#===========================#

**for** name **in** fileName:

#-- Prepare the document to record the table (SNR vs Ampli.)

f = **open**(name + ’.txt’, ’w’)

#-- Load data from the original file rawFile = h5py.File(name + ’.hdf5’, ’r’) strain\_raw = rawFile[’strain/Strain’].value

CBCHIGH\_CAT4 = (rawFile[’quality/simple/DQmask’].value >> 4) & 1

HW\_CBC = (rawFile[’quality/injections/Injmask’].value >> 0) & 1

GPSstart = rawFile[’meta/GPSstart’].value

rawFile.close()

#-- Load the file again which will be injected dataFile = h5py.File(name + ’.hdf5’, ’r+’) strain = dataFile[’strain/Strain’]

dqInj = dataFile[’quality/injections/Injmask’]

#-- Getting the suitable segement lists

segList = rl.dq\_channel\_to\_seglist(CBCHIGH\_CAT4)

segList\_HW = rl.dq\_channel\_to\_seglist(HW\_CBC)

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segList = slice\_filter(segList, segList\_HW)

#-- Pick 10 (or if not more than 10, all) segments randomly

inj\_num = []

**if len**(segList) <= 5:

inj\_num = **range**(0, **len**(segList))

#-- If less than 5, throw a caution

**print** ’Caution: there are less than five suitable spots in %s!’ % name

**print** ’{0} only!’.**format**(**len**(segList))

**else**:

**while len**(inj\_num) < 5:

i = randint(0, **len**(segList)-1)

**if** i **in** inj\_num:

**continue**

inj\_num.append(i)

inj\_num.sort()

List = []

**for** i **in** inj\_num:

List.append(segList[i])

#-- Make and recover injections at each amplitude

**for** k **in range**(0, **len**(A)):

f.write(’{0} ’.**format**(A[k]))

#-- Amplify the template with the difference to next amplification

**if** k == 0:

temp = temp\_strain \* (A[k])

**else**:

temp = temp\_strain \* (A[k] - A[k-1])

#-- Make the injection to every piece

SNRsum = 0

**for** seg **in** List:

#-- Injection starts at the middle

inj\_sample = seg.start + 16\*fs

#-- Superpose the waveform to the signal

**for** j **in range**(0, temp.size):

strain[inj\_sample + j] += temp[j]

#-- Injection Recovery --#

#using the segments in the above section

data = strain[seg]

# to remove effects at the beginning and end of the data stretch, window the data

# https://en.wikipedia.org/wiki/Window\_function#Tukey\_window

**try**: dwindow = sig.tukey(data.size, alpha=1./8) # Tukey window preferred, but

requires recent scipy version

**except**: dwindow = sig.blackman(data.size) # Blackman window OK if Tukey is

not available

#-- Calculate the PSD of the data. Also use an overlap, and window:

# This is where the only change is made, I replaced the PSD of the 32-s segment with

# that of the whole file, because when the file is small the PSD will be greatly

affected by the

# signal in the file, whereas we only want the PSD of the background noise. So taking

the PSD

# of a much larger interval can help eliminating the effect.

data\_psd, freqs = mlab.psd(strain\_raw, Fs = fs, NFFT = NFFT, window=psd\_window,

noverlap=NOVL)

# Take the Fourier Transform (FFT) of the data and the template (with dwindow)

data\_fft = np.fft.fft(data\*dwindow) / fs

#-- Interpolate to get the PSD values at the needed frequencies

power\_vec = np.interp(np.**abs**(datafreq), freqs, data\_psd)

#-- Calculate the matched filter output in the time domain:

# Multiply the Fourier Space template and data, and divide by the noise power in each

frequency bin.

# Taking the Inverse Fourier Transform (IFFT) of the filter output puts it back in

the time domain,

# so the result will be plotted as a function of time off-set between the template

and the data:

optimal = data\_fft \* template\_fft.conjugate() / power\_vec optimal\_time = 2\*np.fft.ifft(optimal)\*fs

#-- Normalize the matched filter output:

# Normalize the matched filter output so that we expect a value of 1 at times of just

noise.

# Then, the peak of the matched filter output will tell us the signal-to-noise ratio

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(SNR) of the signal.

sigmasq = 1\*(template\_fft \* template\_fft.conjugate() / power\_vec).**sum**() \* df sigma = np.sqrt(np.**abs**(sigmasq))

SNR\_complex = optimal\_time/sigma

# shift the SNR vector by the template length so that the peak is at the END of the template

peaksample = **int**(data.size / 2) # location of peak in the template

SNR\_complex = np.roll(SNR\_complex,peaksample)

SNR = **abs**(SNR\_complex)

#-- Find the time and SNR value at maximum:

indmax = np.argmax(SNR)

SNRmax = SNR[indmax]

SNRsum += SNRmax

SNR\_avr = SNRsum / **len**(inj\_num) f.write(’{0}\n’.**format**(SNR\_avr)) dataFile.flush()

**print** ’%s at amplification = {0} finished.’.**format**(A[k]) % name

dataFile.close()

f.close()

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